

In this worksheet you will learn to find the axis of symmetry in a parabola. The axis of symmetry is a vertical line that passes through the vertex of the parabola and is given by  $x = \frac{-b}{2a}$  for a quadratic function  $y = ax^2 + bx + c$ .

## Easy Questions

- 1. Determine the axis of symmetry for the parabola  $y = x^2 + 4x + 3$ .
- 2. Determine the axis of symmetry for the parabola  $y = 2x^2 6x + 5$ .
- 3. Determine the axis of symmetry for the parabola  $y = -x^2 + 2x 1$ .
- 4. Determine the axis of symmetry for the parabola  $y = 3x^2 + 12x + 7$ .
- 5. Determine the axis of symmetry for the parabola  $y = 0.5x^2 2x + 1$ .

## Intermediate Questions

- 6. Find the axis of symmetry for  $y = \frac{1}{2}x^2 + \frac{1}{3}x + 4$ .
- 7. Determine the axis of symmetry for the parabola  $y = 4x^2 16$ .
- 8. Find the axis of symmetry for  $y = -3x^2 9x 2$ .
- 9. A parabola is given by  $y = 5x^2 20x + 3$ . Find its axis of symmetry.
- 10. Determine the axis of symmetry for  $y = 6x^2 + 18x + 7$ .
- 11. Identify the axis of symmetry for  $y = -2x^2 + 4x 6$ .
- 12. For the quadratic function  $y = \frac{3}{4}x^2 \frac{3}{2}x + 8$ , determine the axis of symmetry.
- 13. Calculate the axis of symmetry for  $y = x^2 x + 1$ .
- 14. Rewrite  $y = 2x^2 + 8x + k$  in vertex form and state the axis of symmetry in terms of k.
- 15. Find the axis of symmetry for  $y = -0.5x^2 + x + 10$ .
- 16. Given that the vertex of the parabola  $y = 2x^2 4x + 1$  is (h, k), explain why the axis of symmetry is x = h and find its value.

- 17. Determine the axis of symmetry for  $y = 10x^2 + 5x 3$ .
- 18. If a quadratic function  $y = x^2 + bx + c$  has an axis of symmetry x = 3, determine the value of b.
- 19. Find the axis of symmetry for  $y = 25x^2 50x + 33x^2$
- 20. For the quadratic function  $y = -8x^2 + 32x 15$ , compute the axis of symmetry.

## Hard Questions

- 21. Prove that for a quadratic function  $y = ax^2 + bx + c$  the parabola is symmetric about the line  $x = \frac{-b}{2a}$ .
- 22. A parabola with equation  $y = ax^2 + bx + c$  has its vertex at (2,5) and a = 3. Determine b and hence state the axis of symmetry.
- 23. Determine the axis of symmetry for the function  $y = (x 1)^2 + 3$ .
- 24. A quadratic function passes through the points (0,4), (2,0) and (4,4). Find an equation for this function and state its axis of symmetry.
- 25. A parabola is given by  $y = 7x^2 + bx + 12$  and its axis of symmetry is x = -1. Compute the value of b.
- 26. Show how to rewrite  $y = ax^2 + bx + c$  in vertex form by completing the square and explain how this form confirms that the axis of symmetry is  $x = \frac{-b}{2a}$ .
- 27. Given that a parabola has its axis of symmetry at x = 3 with vertex (3, 1) and passes through (2, 5), determine an equation of the parabola in standard form.
- 28. Show that if a parabola given by  $y = ax^2 + bx + c$  has roots  $r_1$  and  $r_2$ , then the axis of symmetry is given by  $x = \frac{r_1 + r_2}{2}$ .
- 29. For the quadratic function  $y = -2x^2 + bx 3$ , if the axis of symmetry is x = 2.5, find the value of b.
- 30. Let  $y = ax^2 + bx + c$  be a quadratic function. Prove that if the graph is vertically translated by any constant, the axis of symmetry remains  $x = \frac{-b}{2a}$ .